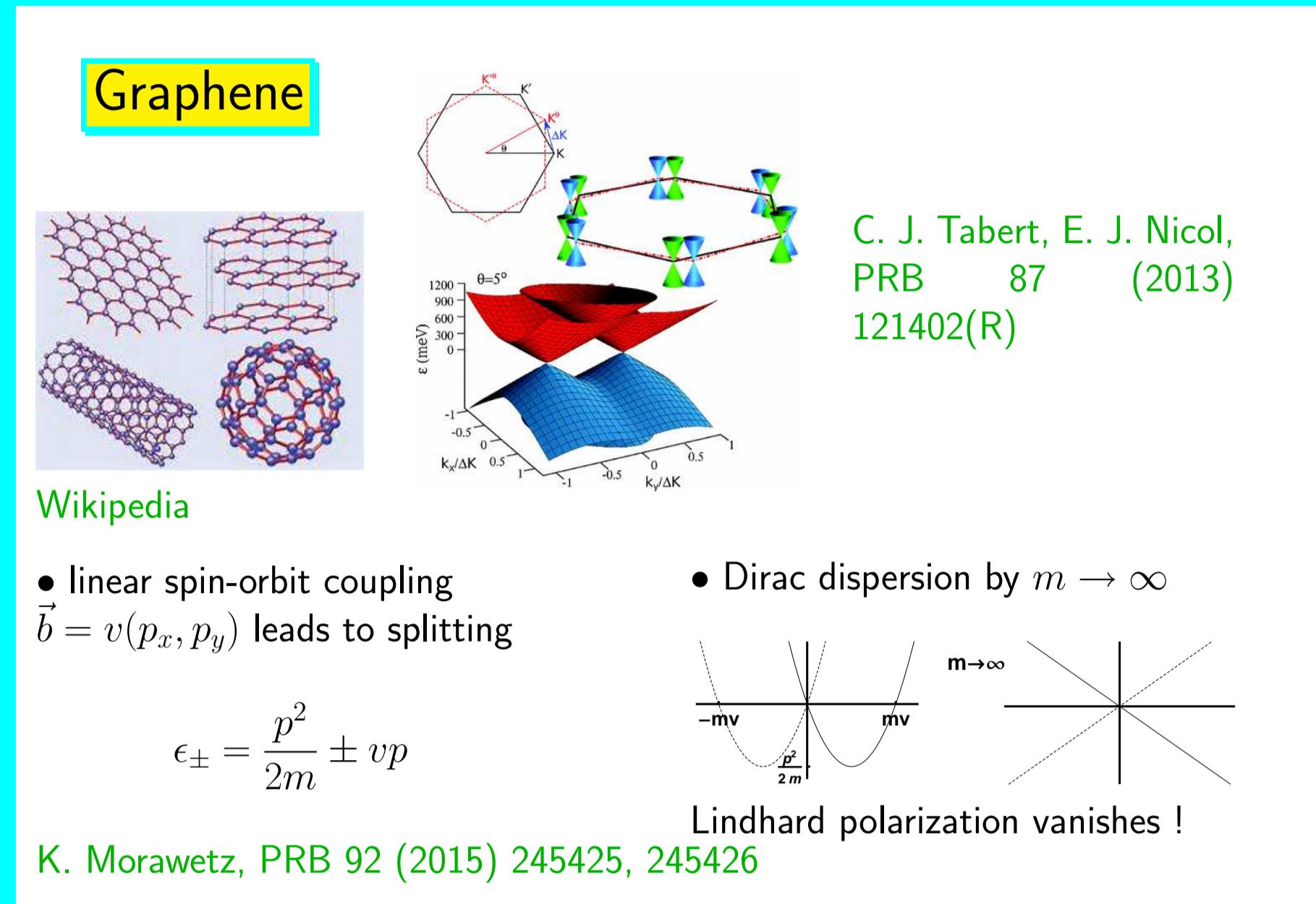


# Currents in graphene and pairing



## Anomalous particle conductivities: universal limits

anomalous particle current  $J_{\alpha} = (\sigma_{\alpha\beta}^{\text{Hall}} + \sigma_{\alpha\beta}^{\text{inter}} + \sigma_{\alpha\beta}^{\text{intra}})E_{\beta}$   
 with  $\mathbf{e} = \Sigma/|\Sigma|$ ,  $g = (f_+ - f_-)/2$

$$\sigma_{\alpha\beta}^{\text{Hall}} = 2e^2 \sum_p \frac{q}{1 - \frac{q^2}{4|\Sigma|^2}} \mathbf{e} \cdot (\partial_{p\alpha} \mathbf{e} \times \partial_{p\beta} \mathbf{e}) \rightarrow \frac{e^2}{8\pi\hbar} \begin{cases} \frac{\Sigma_n}{\mu} + o(\tau_{\omega}^{-1}), & \mu < \Sigma_n \\ \frac{1}{\hbar} + o(\tau_{\omega}^{-1}), & \mu > \Sigma_n \end{cases}$$

$$\sigma_{\alpha\beta}^{\text{intra}} = 2e^2 \sum_p \frac{q}{1 - \frac{q^2}{\omega^2}} \frac{i\omega}{2|\Sigma|^2} \partial_{p\alpha} \mathbf{e} \cdot \partial_{p\beta} \mathbf{e} \rightarrow \zeta \frac{e^2}{16\hbar} \quad (n=0)$$

order of limits		$\sigma_{xx}^{\text{intra}} = \zeta \frac{e^2}{16\hbar}$
5.	4.	3.
$\mu \rightarrow 0$	$\omega \rightarrow 0$	$\Sigma \rightarrow 0$
$\mu \rightarrow 0$	$\tau \rightarrow \infty$	$\Sigma \rightarrow 0$
$\tau \rightarrow \infty$	$\mu \rightarrow 0$	$\Sigma \rightarrow 0$
$\mu \rightarrow 0$	$\Sigma \rightarrow 0$	$\tau \rightarrow \infty$
$\mu \rightarrow 0$	$\tau \rightarrow \infty$	$\omega \rightarrow 0$
$\mu \rightarrow 0$	$\omega \rightarrow 0$	$\Sigma \rightarrow 0$
$\mu \rightarrow 0$	$\tau \rightarrow \infty$	$\omega \rightarrow 0$
$\mu \rightarrow 0$	$\omega \rightarrow 0$	$\tau \rightarrow \infty$
$\mu \rightarrow 0$	$\Sigma \rightarrow 0$	$\omega \rightarrow 0$
$\mu \rightarrow 0$	$\omega \rightarrow 0$	$\tau \rightarrow \infty$
$\mu \rightarrow 0$	$\Sigma \rightarrow 0$	0

• chiral nature of charge carriers leads to minimal finite conductivity even with vanishing density of scatterers

• field has to create first electron-hole pairs before they can be accelerated

$$\sigma_{\alpha\beta}^{\text{intra}} = i2e^2 \sum_p \partial_{p\alpha} \partial_{p\beta} \frac{q}{\omega} = \frac{ie\omega_p^2(n, \Sigma_n)}{\omega + \frac{i}{\tau}}$$

## Pseudospin conductivity

pseudospin current  $S_{\alpha} = 2 \sum_p (\partial_{p\alpha} \epsilon \delta g + \delta f \partial_{p\alpha} \mathbf{b})$ , normal spin-Hall

$$\sigma_{\alpha\beta}^{\text{as}} = \frac{e}{m_e \omega} \sum_p \frac{p_{\alpha} g}{1 - \frac{\omega^2}{4|\Sigma|^2}} \left\{ \begin{array}{l} \frac{i\omega}{2|\Sigma|} \mathbf{e} \times \partial_{p\beta} \mathbf{e} \\ i \partial_{p\beta} \mathbf{e} \end{array} \right\}$$

with  $\omega \rightarrow \omega + i/\tau$ , for zero temperature and linear Rashba coupling

$$\sigma_{yx}^z = \frac{e}{8\pi\hbar} \left[ 1 - \frac{\hbar^2 + 4\Sigma_n^2 \tau_{\omega}^2}{4e\tau_{\omega}\hbar} \arctan \left( \frac{4\hbar e\tau_{\omega}}{\hbar^2 + 4\tau_{\omega}^2(2e\mu + \Sigma_n^2)} \right) \right]$$

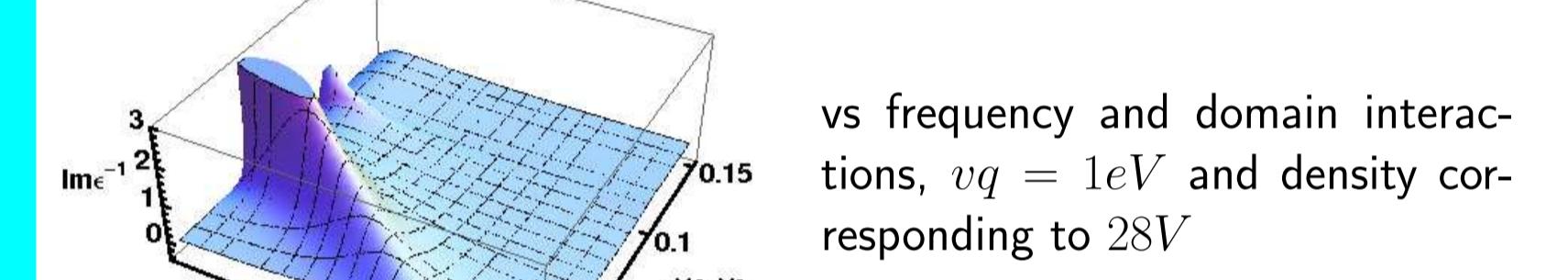
$$\sigma_{xx}^z = \frac{2}{\hbar} \Sigma_n \tau \sigma_{yx}^z$$

with  $\tau_{\omega} = \tau/(1 - i\omega\tau)$  and  $\epsilon_v = mv^2$

for graphene limit of infinite mass universal value  $\lim_{m \rightarrow \infty} \sigma_{yx}^z = \frac{e}{8\pi\hbar}$  contrary to expectation vanishing normal parts of pseudospin current

## Density response function

induced density  $\delta n = \chi \Phi^{\text{ext}}$ , inverse dielectric function  $\frac{1}{\epsilon} = \frac{V^s}{\Phi^{\text{ext}}} = 1 + V_0 \chi$

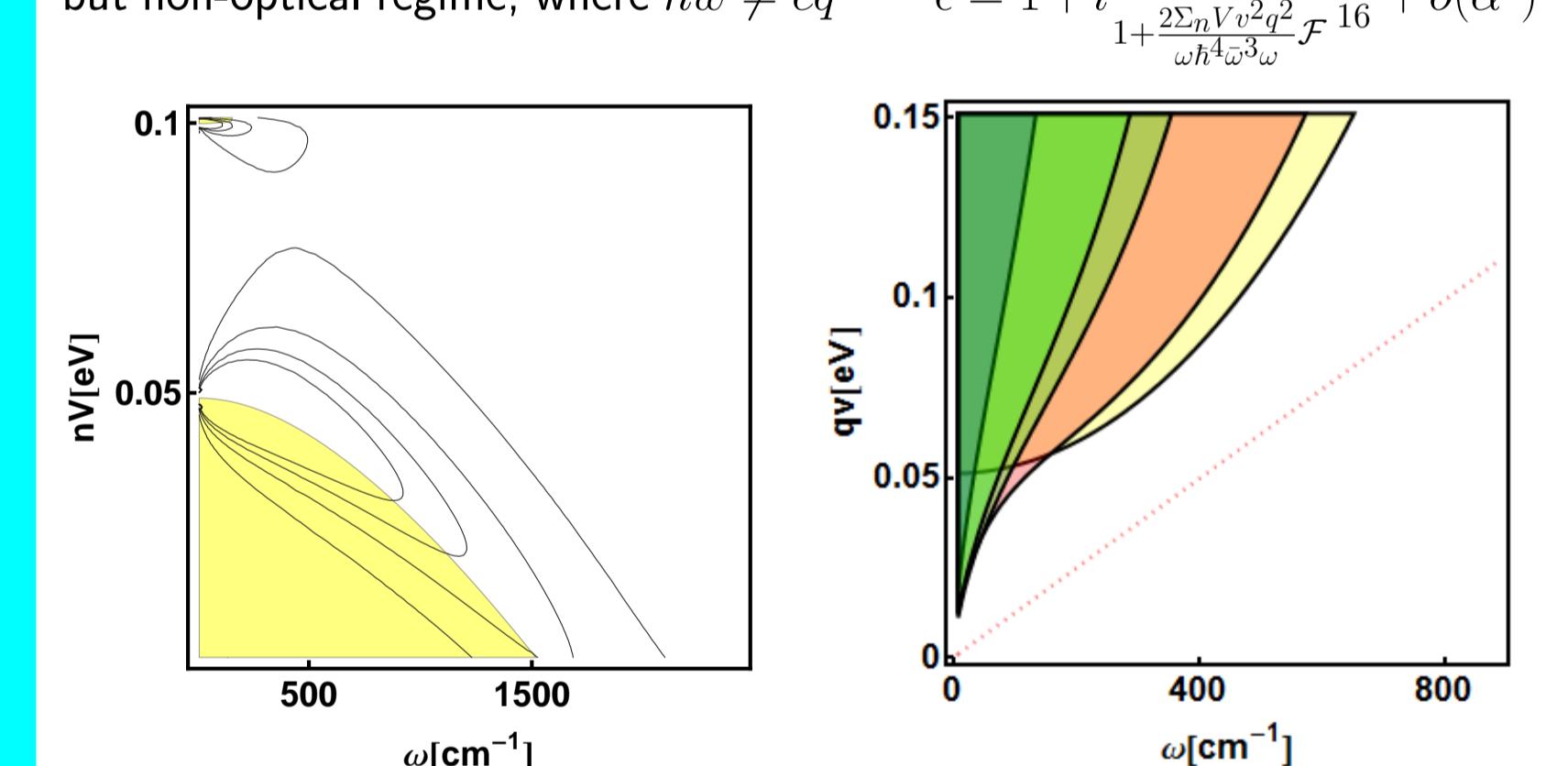


- with increasing magnetic domain strength  $V$  collective peak sharpened and shifted towards lower frequencies, second peak around  $V = 0.1$  is at the line  $\mu \leq \Sigma_n$
- small parameter  $\eta = \frac{vq}{\hbar\omega} = \frac{1}{300}$  in the optical regime cannot lead to any sign change

$$\frac{1}{\epsilon} = 1 - \frac{\omega}{\omega} \eta^2 - i \frac{\omega^2}{\omega^2} \frac{\pi\alpha}{16} \eta^3 + o(\eta^4)$$

## Sign change of dielectric function

but non-optical regime, where  $\hbar\omega \neq cq$

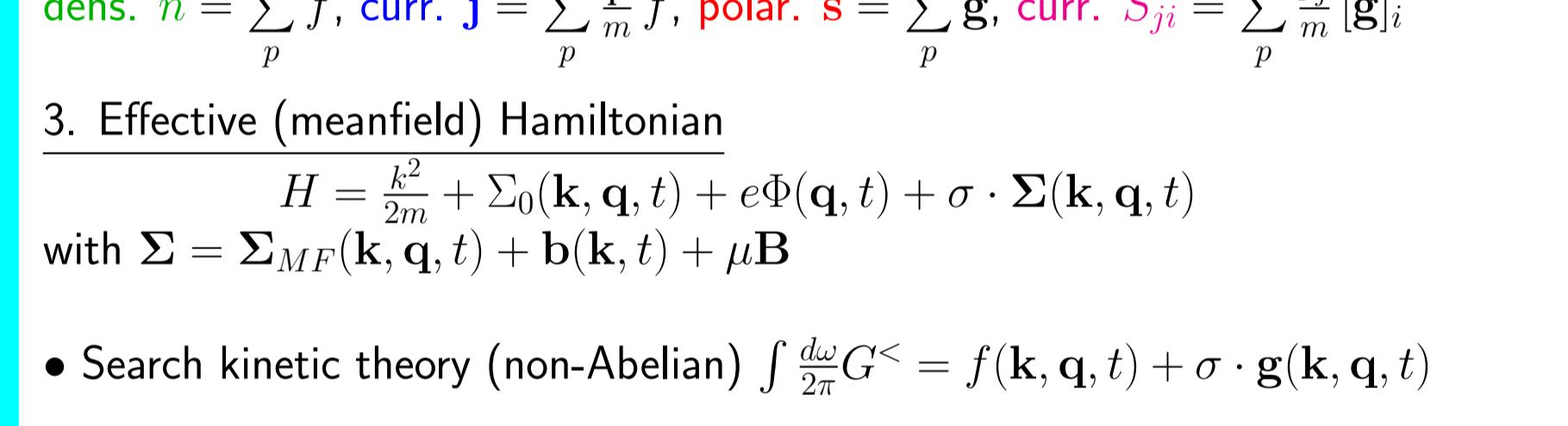


- sign change is a prerequisite for Cooper pairing

## Summary

- Coupled quantum kinetic equation for systems with SU(2) structure:
  - mean field interaction (scalar+vector), suited for magnetized impurities, spin-flip, ..
  - arbitrary magnetic and electric fields, spin-orbit interaction
- anomalous currents in graphene as infinite mass limit of spin-orbit coupling
- influence of magnetic domain puddles and meanfields recast into effective Zeeman field on intra-, interband longitudinal and Hall conductivities
- density-independent universal conductivity for large Zeeman fields or small densities
- experimental optical conductivity well reproduced by intrinsic effective Zeeman field
- pseudospin current non-trivially universal value though quasiparticle velocity vanishes
- effective Zeeman field leads to frequency and wavelength range where screened interaction changes sign allowing Cooper pairs

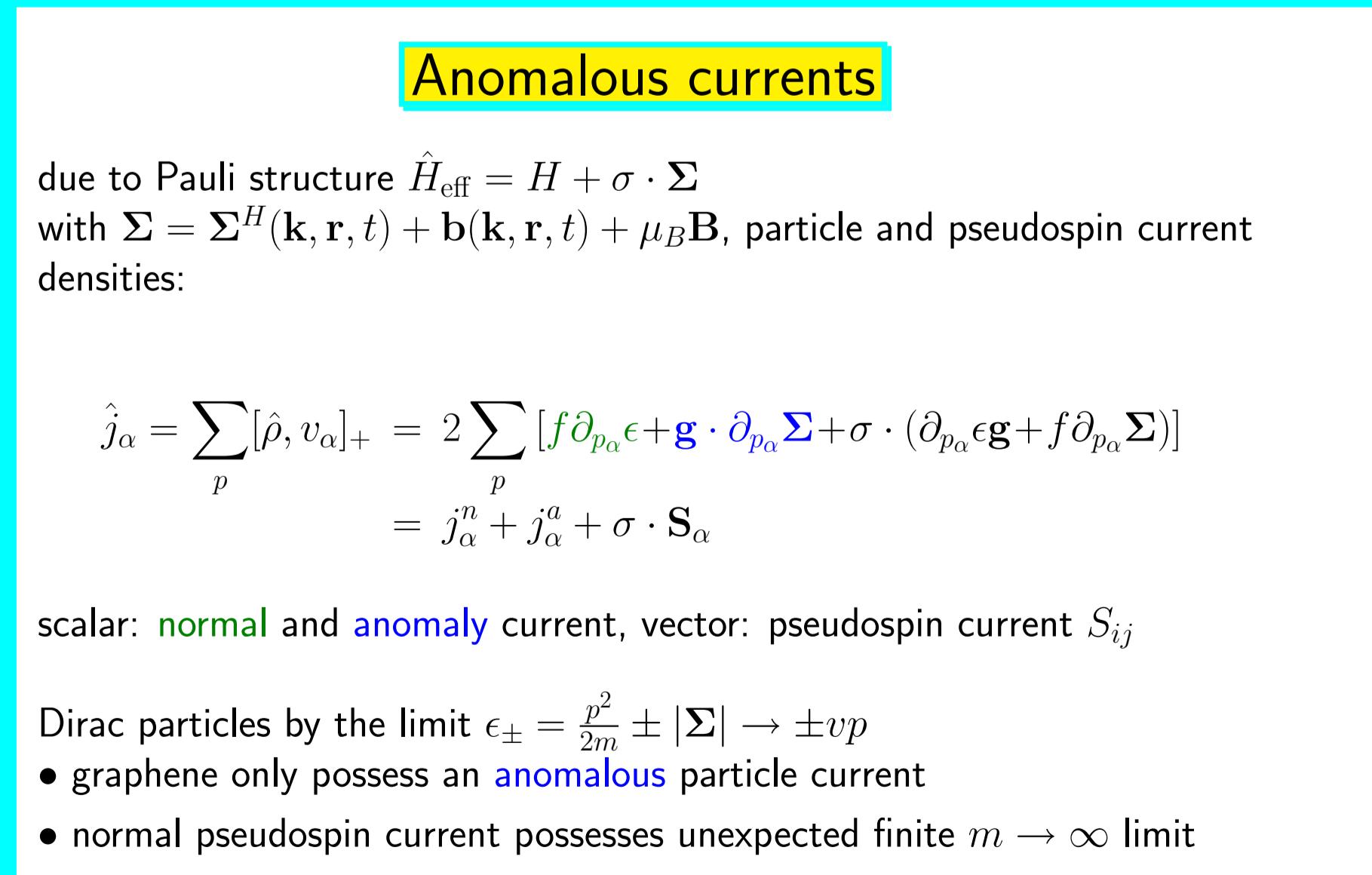
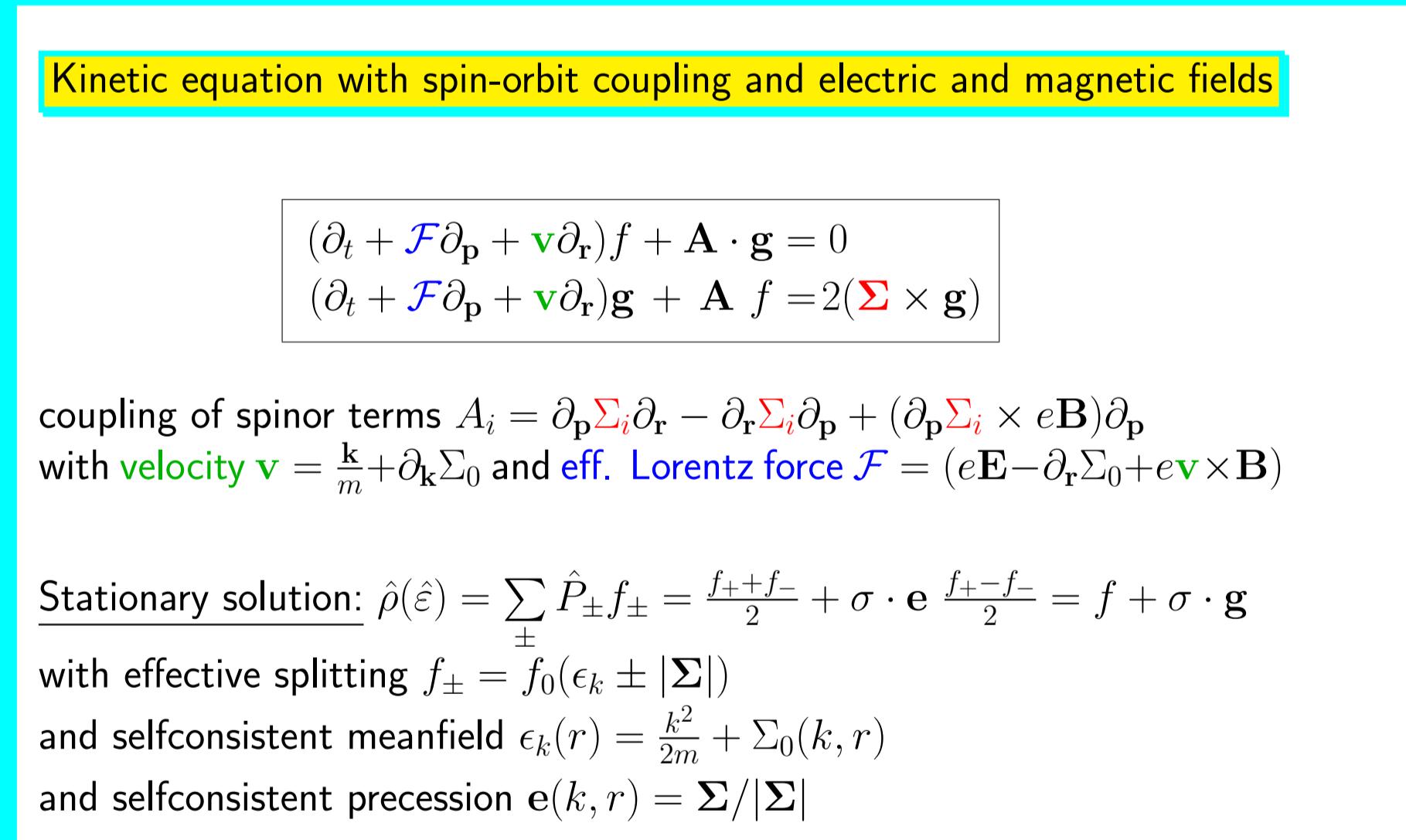
- Europhys. Lett., 104 (2013) 27005: *Terahertz out-of-plane pulses due to spin-orbit coupling*
- *Quantum kinetic theory of spin-polarized systems in electric and magnetic fields with spin-orbit coupling*: Phys. Rev. B 92 (2015) 245426: I. Kinetic equation and anomalous Hall and spin-Hall effects, Phys. Rev. B 92 (2015) 245426: II. RPA response functions and collective modes
- Phys. Rev. B 94 (2016) 165415: *Dynamical charge and pseudospin currents in graphene and possible Cooper pair formation*



Extrinsic spin-orbit coupling meanfield more involved  
 $\Sigma_0^{\text{ext}} = i\frac{q^2}{\hbar^2} V [m(\mathbf{S}_j \times \mathbf{q}_j) - \mathbf{s} \cdot (\mathbf{p} \times \mathbf{q})], \Sigma^{\text{ext}} = i\frac{q^2}{\hbar^2} V [m(\mathbf{j} \times \mathbf{q}) - \mathbf{n}(\mathbf{p} \times \mathbf{q})]$   
 dens.  $\mathbf{n} = \sum_f f, \mathbf{curr. j} = \sum_p p, \mathbf{polar. s} = \sum_g g, \mathbf{curr. S} = \sum_p p/m_g [\mathbf{g}]$

3. Effective (meanfield) Hamiltonian  
 $H = \frac{k^2}{2m} + \Sigma(\mathbf{k}, \mathbf{q}, t) + e\Phi(\mathbf{q}, t) + \sigma \cdot \Sigma(\mathbf{k}, \mathbf{q}, t)$   
 with  $\Sigma = \Sigma_{MF}(\mathbf{k}, \mathbf{q}, t) + \mathbf{b}(\mathbf{k}, t) + \mu_B \mathbf{B}$

• Search kinetic theory (non-Abelian)  $\int \frac{d\omega}{2\pi} G^< = f(\mathbf{k}, \mathbf{q}, t) + \sigma \cdot g(\mathbf{k}, \mathbf{q}, t)$



## Optical conductivity

Experimental values (dots) Z. Q. Li et al., Nature Physics 4, 532 (2008)

